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## K-Theory, Quadratic Forms and Number Theory Seminar

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Dr John Cosgrave (<http://staff.spd.dcu.ie/johnbcos/>)

will speak on

### Extensions of the Gauss-Wilson theorem

Wed 26th March 2008 at 5:00PM

Location: Mathematical Sciences Seminar Room

Karl Dilcher and I have made the first extension of the G-W theorem since the appearance of Gauss' Disquisitiones. Defining  $N_n!$  – the 'Gauss factorial' of  $N$  with respect to – to be the product of the residue classes in  $[1, N]$  that are relatively prime to  $n$ , we have given a complete determination of the order of  $(N_n!) \pmod{n}$ . This is a composite modulus extension of Mordell's 1961 result concerning the order of  $(p-1/2)! \pmod{p}$  (prime  $p$ ).

I will outline work-in-progress concerning the order of  $(n-1/M)_n! \pmod{n}$  for  $M = 3$  and  $4$ , introduce a new class of primes (Gauss primes), and outline a number of open problems.

This talk is part of the **K-Theory, Quadratic Forms and Number Theory** series. For more, see <https://maths.ucd.ie/seminars>