



Seminar

## K-Theory, Quadratic Forms and Number Theory

**Title:** Gauss' Method for determining cyclotomic numbers

**Speaker:** Dr. Ciaran Mac an Bhaird (NUIM)

**Date:** Wed 21st November 2007 at 4:00PM

**Location:** Mathematical Sciences Seminar Room

**Abstract:** We will discuss how Gauss' method leads to a series of functional equations. We have necessary and sufficient conditions for these equations to have integer solutions. This leads to a purely Diophantine system of equations, the number of equations is independent of the prime  $p$ , where  $p$  is congruent to 1 modulo  $l$ . The system has precisely  $\phi(l)$  solutions, which correspond to the cyclotomic numbers of order  $l$ . Using this method, we will go through the cyclotomic numbers of order 3, 5 and 7 and discuss some interesting aspects of these and further orders.