



## Analysis Seminar

**Title:** Fischer decomposition for entire functions and the Dirichlet problem for unbounded quadratic surfaces

**Speaker:** Hermann Render

**Date:** Tue 25th October 2022 at 3:00PM

**Location:** Seminar Room SCN 1.25

**Abstract:** Let  $P_{2k}$  be a homogeneous non-negative polynomial of degree  $2k$  and assume that  $P_j$  for  $j=0, \dots, \beta < 2k$  are homogeneous polynomials of degree  $j$ . Further a certain integral inequality depending on a parameter  $\alpha$  and  $P_{2k}$  is assumed which is valid for all homogeneous polynomials of degree  $m$ .

The main result of the talk states that for any entire function  $f$  of order

$\rho < (2k - \beta)/\alpha$  there exist entire functions  $q$  and  $r$

of finite order with

$f = (P_{2k} - P_\beta - \dots - P_0)q + r$  and  $\Delta^k r = 0$

where  $\Delta$  is the Laplace operator.

This result is used to establish the existence of entire harmonic solutions of the Dirichlet problem for cylinders and parabola-shaped domains for data given by entire functions of order smaller than 1 and  $1/2$  respectively.

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