

UCD School of Mathematics and Statistics

University College Dublin Belfield, Dublin 4, Ireland

Tel +353 1 716 2580 Fax +353 1 716 1196

Scoil na Matamaitice agus na Staitisticí UCD

An Coláiste Ollscoile, Baile Átha Cliath Belfield, Baile Átha Cliath 4, Éire

Email seminars@maths.ucd.ie
Web maths.ucd.ie/seminars

Analysis Seminar

Richard Smith

will speak on

A topological characterization of dual strict convexity in Asplund spaces I

Tue 23rd April 2019 at 4:20PM

Location: Seminar Room SCN 1.25

In 1975 Lindenstrauss asked whether it is possible to characterize Banach spaces X that admit an equivalent strictly convex norm, in terms of other linear or topological properties of X. We provide a partial answer to this problem in the case of dual spaces, by showing that if X is an Asplund space, then it admits an equivalent norm having a strictly convex dual norm if and only if the dual unit sphere S_{X^*} (equivalently X^*), endowed with the w^* -topology, possesses a certain topological property. It follows that this ostensibly geometric property of the space can in fact be characterised in purely non-linear, topological terms.

In the first of two talks we will cover the background to the problem, the basic concepts involved, and give an introduction to the main technique of the proof, which is a type of set-theoretic derivation or 'eating' process. Such processes are usually indexed by natural numbers or ordinal numbers, but this one is indexed instead by elements of a certain tree.

This talk is part of the **Analysis** series. For more, see https://maths.ucd.ie/seminars