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## Analysis Seminar

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**R. Smith**

will speak on

### Approximation of norms in Banach spaces

Tue 6th February 2018 at 4:00PM

Location: SCN 125

This talk follows on from one I gave in May 2017. Let  $X$  be a Banach space and let  $\mathbf{P}$  be a property of norms. We say that a norm  $\|\cdot\|$  on  $X$  (equivalent to the original norm) can be approximated by norms having  $\mathbf{P}$  if, given  $\varepsilon > 0$ , there exists another norm  $\|\cdot\|'$  on  $X$  with  $\mathbf{P}$ , such that  $\|x\| \leq \|x\|' \leq (1 + \varepsilon)\|x\|$  for all  $x \in X$ . There are a number of papers in the literature that consider the question of whether or not all (equivalent) norms on a given space can be approximated in this way. For a number of classes of Banach spaces  $X$ , including  $c_0(\Gamma)$  (where  $\Gamma$  is an arbitrary set), certain Orlicz spaces and Lorentz predual spaces, and a class of  $C(K)$  spaces (where  $K$  comes from a class of compact spaces having unbounded scattered height), we show that all equivalent norms on  $X$  can be approximated by  $C^\infty$ -smooth norms or polyhedral norms. This is joint work with Stanimir Troyanski, University of Murcia, Spain, and Institute of Mathematics, Bulgarian Academy of Sciences.

This talk is part of the **Analysis** series. For more, see  
<https://maths.ucd.ie/seminars>