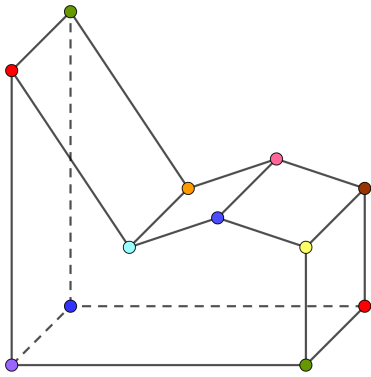
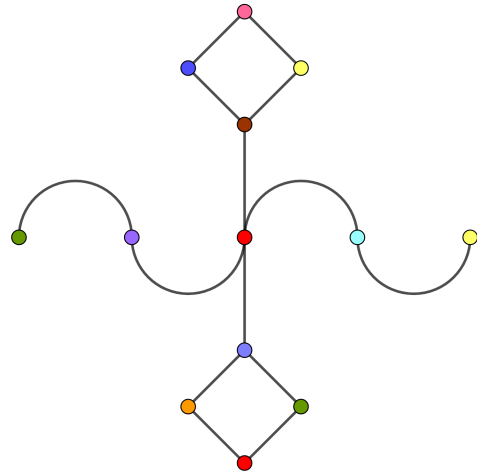


$$\mathbf{V} + \mathbf{F} - \mathbf{E} = \square$$


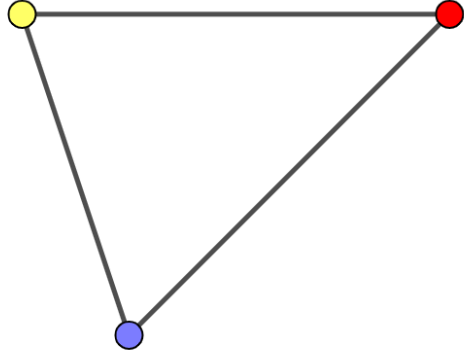


$$\mathbf{V} + \mathbf{F} - \mathbf{E} = \square$$

# Graph Theory



A **graph** is a collection of **vertices** connected by **edges**.

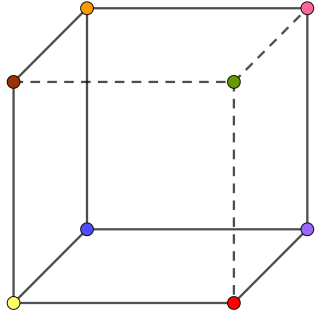



This graph has  
3 **V**ertices  
3 **E**dges

and it divides the page into  
2 **R**egions

2

Let's try a 3D graph.  
For 3D graphs, instead of regions we use **faces**.

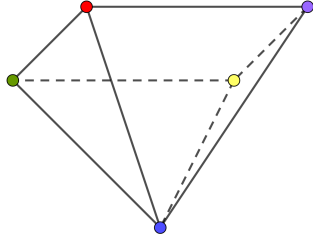


$$\square = \square + \square - \square - \square + \square$$

**V**                      **F**                      **E**

Does the pattern continue?

Try some more 3D graphs:



$$\square = \square + \square - \square - \square + \square$$

**V**                      **F**                      **E**

2

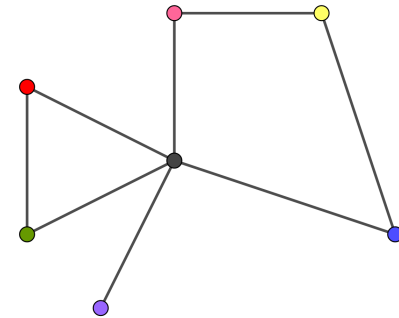
Design your own graph, and see if the pattern continues!

My graph:

Leonhard Euler is a famous mathematician, who made an important discovery in graph theory. He discovered something interesting when he calculated:

$$\begin{array}{ccccccc} \mathbf{V} & + & \mathbf{R} & - & \mathbf{E} & & \\ \text{number of vertices} & & \text{number of regions} & & \text{number of edges} & & \end{array}$$

Let's calculate it for this graph:

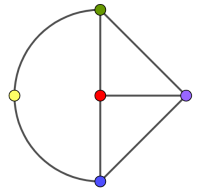


$$\begin{array}{ccccccc} \mathbf{V} & + & \mathbf{R} & - & \mathbf{E} & & \\ \square & + & \square & - & \square & = & \square \end{array}$$

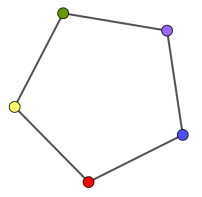
$$\begin{array}{ccccccc} \mathbf{V} & + & \mathbf{R} & - & \mathbf{E} & & \\ \square & + & \square & - & \square & = & \square \end{array}$$

4

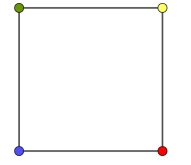
$$\square = \square_V + \square_R - \square_E$$



$$\square = \square_V + \square_R - \square_E$$



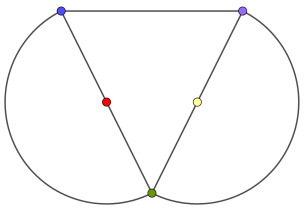
$$\square = \square_V + \square_R - \square_E$$



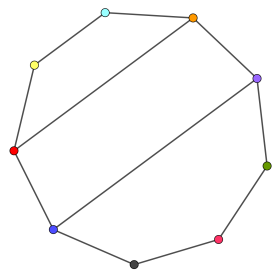
Now you try some!

5

$$\square = \square_V + \square_R - \square_E$$



$$\square = \square_V + \square_R - \square_E$$



$$\square = \square_V + \square_R - \square_E$$

