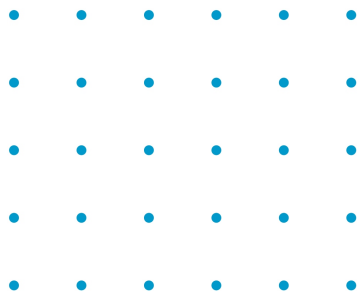


$$\frac{B}{2} + I - 1 = \text{Area}$$

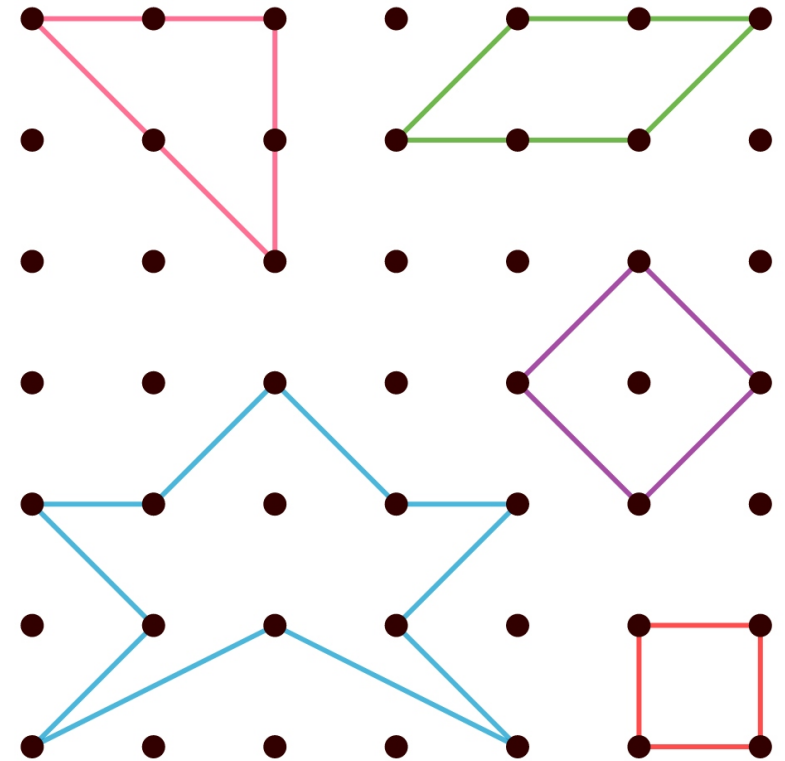
$\square + \square - 1 = \square$  square units

Now draw your own shape, and calculate the area!



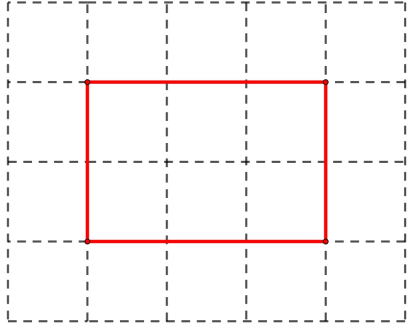
$$\frac{B}{2} + I - 1 = \text{Area}$$


$\square + \square - 1 = \square$  square units



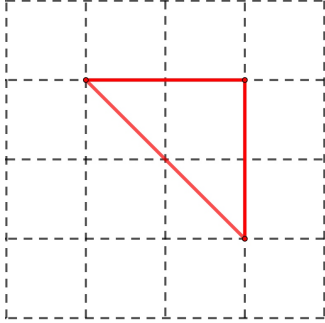
# Geoboards & Pick's Theorem

Can you calculate the area of this rectangle by counting the squares, or otherwise?






Area =  square units

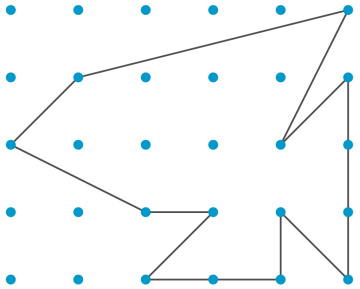
What about this triangle?






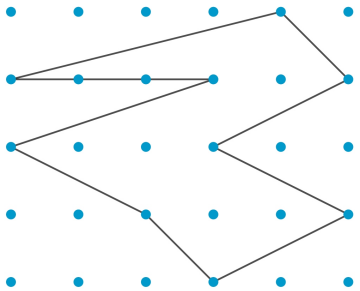
Area =  square units

2

Area =  +  -  square units

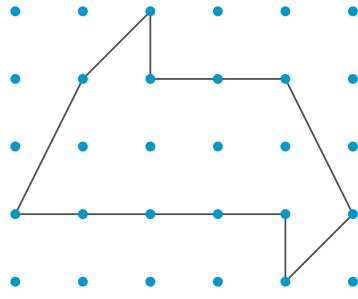


Area =  +  -  square units



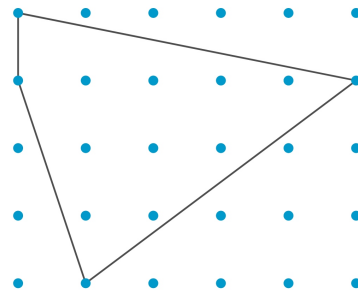
1

Now try some yourself!



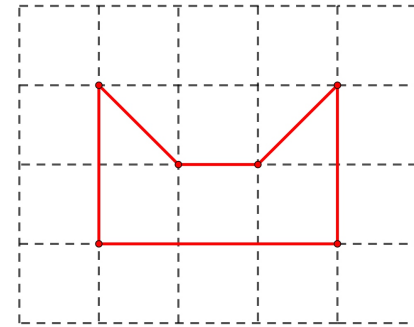
$\frac{B}{2}$       **I**      **Area**

+  - 1 =  square units



$\frac{B}{2}$       **I**      **Area**

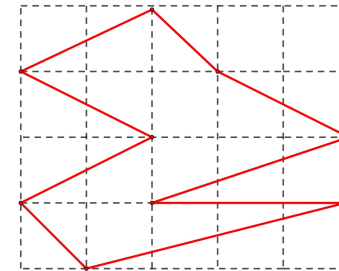
+  - 1 =  square units



**Area** =  square units



But it's much harder to find the area of unusual shapes, like this one:



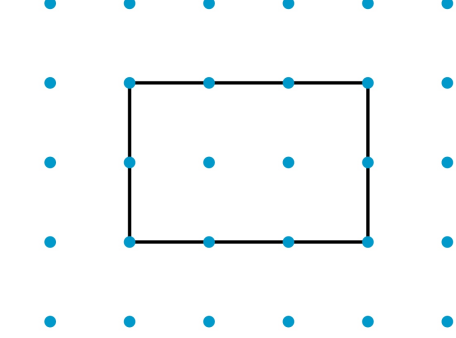
I wonder if there is an easier way to find the area of more complex shapes?

A mathematician called Georg Alexander Pick discovered something special about shapes on geoboard...

$$\text{Area} = \frac{B}{2} + I - 1$$

half the number of boundary points + the number of interior points

Let's try a shape together:



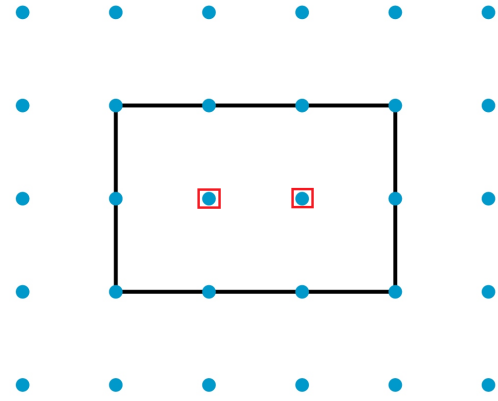
$$B = I = 1$$

Area

$$\frac{B}{2} + I - 1 = \text{Area}$$

square units

When you make a shape on a geoboard, the points inside the shape are called **interior points**.



The points that the lines pass through are called **boundary points**.

