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The distinction is quite striking, as shown in the following figure.



Calculate the radiative equilibrium temperature of the earth's surface and atmosphere assuming that the atmosphere can be regarded as a thin layer with an absorbtivity of 0.1 for solar radiation and 0.8 for terrestrial radiation.

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Assume that the earth's surface radiates as a blackbody at all wavelengths. Also assume that the net solar irradiance absorbed by the earth-atmosphere system is $F = 241 \text{ W m}^{-2}$.

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Assume that the earth's surface radiates as a blackbody at all wavelengths. Also assume that the net solar irradiance absorbed by the earth-atmosphere system is $F = 241 \text{ W m}^{-2}$.

Explain why the surface temperature computed above is considerably higher than the effective temperature in the absence of an atmosphere.

The incoming flux of solar radiation at the top of the atmosphere is $F_S = 240 \text{ W m}^{-2}$.

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Since the absorbtivity for solar radiation is 0.1, the downward flux of short wave radiation at the surface is $0.9 \times F_S$.

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Let F_E be the long wave flux emitted upwards by the surface.

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Since the absorbtivity for terrestrial radiation is 0.8, there results an upward flux at the top of the atmosphere of $0.2 \times F_E$.

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Let F_L be the long wave flux emitted upwards by the atmosphere; this is also the long wave flux emitted *downwards*.

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Thus, the total downward flux at the surface is $0.9 \times F_S + F_L$.

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Let F_L be the long wave flux emitted upwards by the atmosphere; this is also the long wave flux emitted *downwards*. Thus, the total downward flux at the surface is $0.9 \times F_S + F_L$. This must equal the upward flux from the surface:

$$F_E = 0.9 \times F_S + F_L$$

 $F_S = 0.2 \times F_E + F_L$

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To find F_E and F_L , we must solve the system of simultaneous equations

$$F_L - F_E = -0.9F_S$$

$$F_L + 0.2F_E = F_S$$

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This gives the values

$$F_E = \frac{1.9}{1.2} \times F_S = 380 \,\mathrm{W}\,\mathrm{m}^2$$
 $F_L = \frac{0.82}{1.2} \times F_S = 164 \,\mathrm{W}\,\mathrm{m}^2$

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$$\sigma T_{\text{surface}}^4 = F_E = 380 \,\text{W}\,\text{m}^2$$

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$$\sigma T_{\text{surface}}^4 = F_E = 380 \,\text{W}\,\text{m}^2$$

Therefore, since $\sigma = 5.67 \times 10^{-8} \,\mathrm{W} \,\mathrm{m}^{-2} \mathrm{K}^{-4}$, we have

$$T_{\text{surface}} = \sqrt[4]{\frac{380}{5.67 \times 10^{-8}}} = 286 \,\text{K} = +13^{\circ}\text{C}$$

$$0.8\,\sigma T_{\rm atmos}^4 = 164\,{\rm W\,m^2}$$

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$$T_{\rm atmos} = \sqrt[4]{\frac{164}{5.67 \times 10^{-8}}} = 245 \,\mathrm{K} = -28^{\circ}\mathrm{C}$$

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Note that the surface temperature in this case is some 31° C higher than in the case of exercise 4.6 when there was no atmosphere:

$$T_{\text{surface}} = +13^{\circ}\text{C}$$

 $T_{\text{atmos}} = -28^{\circ}\text{C}$

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Note that the surface temperature in this case is some 31° C higher than in the case of exercise 4.6 when there was no atmosphere:

$$T_{\text{surface}} = +13^{\circ}\text{C}$$

 $T_{\text{atmos}} = -28^{\circ}\text{C}$

No atmosphere:

$$T_{\text{surface}} = -18^{\circ}\text{C}$$

Consider a planet with an atmosphere consisting of multiple isothermal layers, each of which is transparent to shortwave radiation and completely opaque to longwave radiation.

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The layers are in radiative equilibrium with one another and with the surface of the planet.

Show how the surface temperature of the planet is affected by the presence of this atmosphere and describe the radiative equilibrium temperature profile in the atmosphere of the planet.

Begin by considering an atmosphere comprised of a single isothermal layer.

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Since the layer is isothermal, it also emits F units of radiation in the downward radiation.

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Hence, the downward radiation at the surface of the planet is F units of incident solar radiation plus F units of longwave radiation emitted from the atmosphere, a total of 2F units,

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Hence, the downward radiation at the surface of the planet is F units of incident solar radiation plus F units of longwave radiation emitted from the atmosphere, a total of 2F units,

This must be balanced by an upward emission of 2F units of longwave radiation from the surface.

If a second isothermal, opaque layer is added, the flux density of radiation upon the lower layer will be 2F (F units of solar radiation plus F units of longwave radiation emitted by the upper layer).

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To balance the incident radiation, the lower layer must emit 2F units of longwave radiation. Since the layer is isothermal, it also emits 2F units of radiation in the downward radiation.

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To balance the incident radiation, the lower layer must emit 2F units of longwave radiation. Since the layer is isothermal, it also emits 2F units of radiation in the downward radiation.

Hence, the downward radiation at the surface of the planet is F units of incident solar radiation plus 2F units of longwave radiation emitted from the atmosphere, a total of 3Funits, which must be balanced by an upward emission of 3Funits of longwave radiation from the surface.



Radiation balance for a planetary atmosphere that is transparent to solar radiation and consists of two isothermal layers that are opaque to planetary radiation.

The emissions from the atmospheric layers, working downward from the top, are F; 2F; 3F:::NF and the corresponding radiative equilibrium temperatures are 255, 303, 335.... $(F/N\sigma)^{1/4}$ K.

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To estimate the corresponding radiative equilibrium lapse rate within the atmosphere we would need to take into account the fact that the geometric thickness of opaque layers decreases rapidly as one descends through the atmosphere owing to the increasing density of the absorbing media with depth.

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Hence, the radiative equilibrium lapse rate steepens with increasing depth.

In effect, radiative transfer becomes less and less efficient at removing the energy absorbed at the surface of the planet due to the increasing blocking effect of the greenhouse gases. Once the radiative equilibrium lapse rate exceeds the adiabatic lapse rate, convection becomes the primary mode of energy transfer. Once the radiative equilibrium lapse rate exceeds the adiabatic lapse rate, convection becomes the primary mode of energy transfer.

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The bottom panel of Fig. 4.5 shows that the wavelength dependence is quite pronounced, with well defined *absorption bands* identified with specific gaseous constituents, interspersed with *windows* in which the atmosphere is relatively transparent.

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- In fact, the main process balancing incoming solar radiation at the earth's surface is evaporation.
- The water evaporated from the ocean is carried upward by convection.
- The moisture reaches levels above the main infra-red absorbers.
- The latent heat is then released by condensation, from where much of it radiates to space.

End of §4.3